

# GSSHA Snow Modeling Capabilities



- Water Supply in the Western United States
  - Meltwater from the snowpack in the headwaters can provide 50-80% of the annual downstream water supply (Wahl, 1992).
  - Headwater catchments compose less than 25% of the total land area, but snowmelt from these areas provide roughly 70% of the annual runoff (Barros & Lettenmaier, 1993).
- Hydrograph Timing
  - Snow has the effect of changing the timing of annual streamflow
  - Instead of the rapid rainfall runoff response in non-snow dominated regions, water is stored in the snowpack until the spring/summer thaw period
- Flooding
  - In the upper midwestern United States US rainfall on snow events produce the largest, and most damaging, flooding events

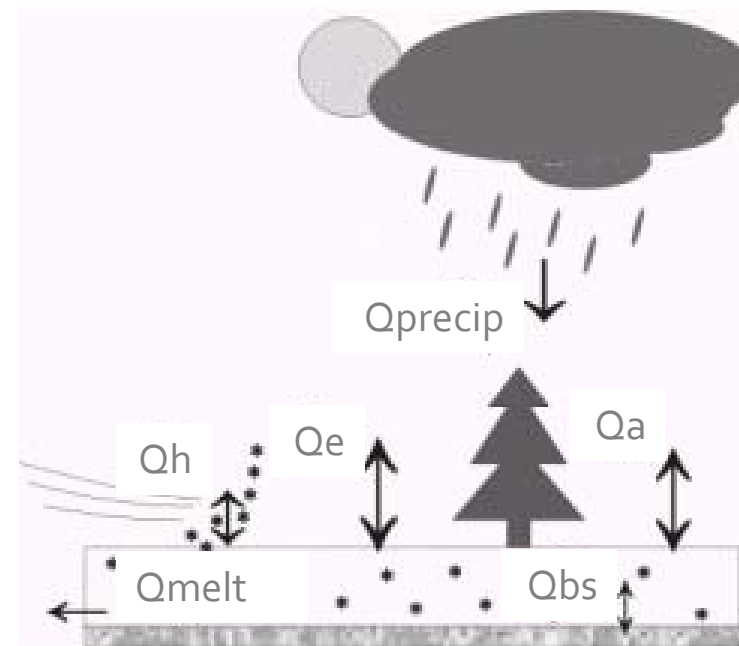




- Modeling of Snow Water Equivalent (SWE)
  - Four snow-pack melt models
    - Energy Balance
    - Temperature-Index
    - Hybrid Energy Balance
    - Radiation-derived Temperature-Index
  - Accounting for snow-pack dynamics
- Adjustments to Hydro-meteorological Forcing (HMET) Data
- Melt Water Transport
  - Vertical flow through snow-pack
  - Lateral flow through snow-pack
  - Frozen soil impedes infiltration



- Energy Balance (EB) – accounts for the energy fluxes between the snow-pack, ground, atmosphere, and precipitation. If enough energy is input into the snow-pack then melting occurs.
- Temperature-Index (TI) – The amount of melt within the snow-pack is based on the temperature, precipitation, and calibrated parameters. Based on SNOW-17 model.
- Hybrid Energy Balance (HY - **Default**) – modification of the Energy Balance model that accounts for snow-pack temperature dynamics (heat deficits).
- Radiation-Derived Temperature-Index (RTI) – Also based on SNOW-17, but uses a radiation-derived proxy temperature instead of air temperature in the melt equations.



Picture Adapted from: Tarboton 1996

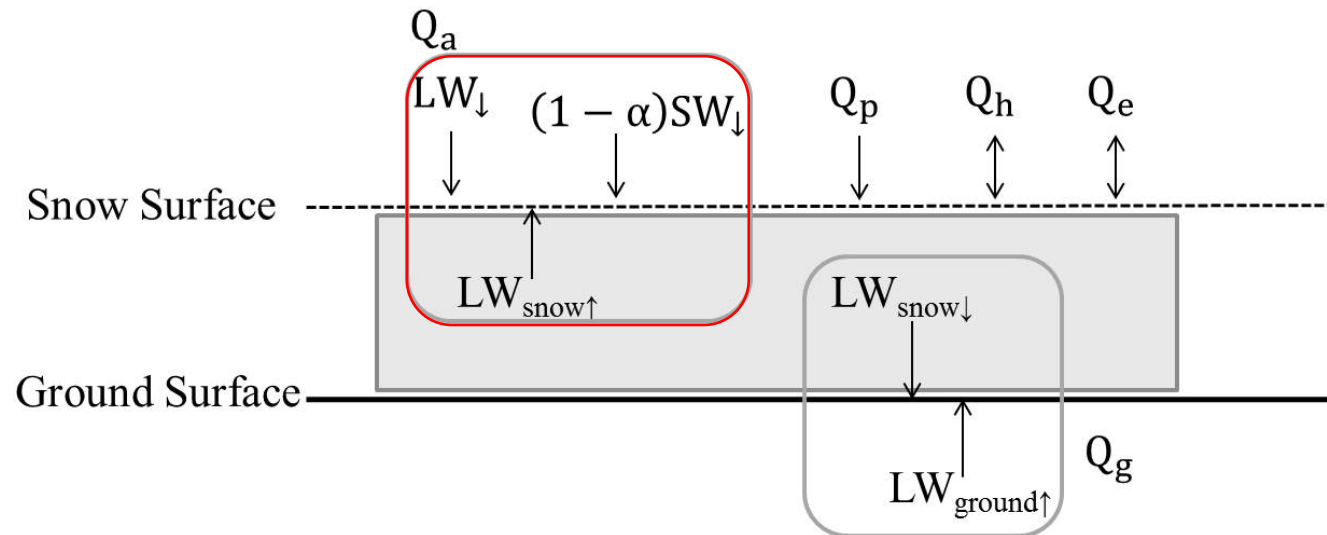


Snow Energy Balance (EB)

$$Melt = \frac{\sum Q}{L_f} dt$$

Temperature Index (TI)

$$Melt = M_f T_a dt$$

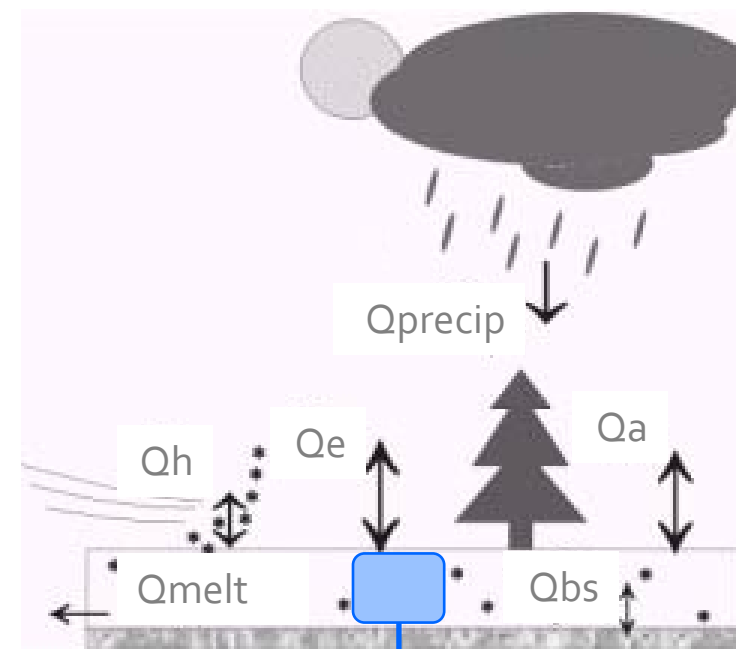


$Q_a$  – Net Radiation  
 $Q_p$  – Precipitation Heat Flux  
 $Q_h$  – Sensible Heat Flux  
 $Q_e$  – Latent Heat Flux  
 $Q_g$  – Ground Heat Flux  
 $\sigma$  – Stefan Boltzmann Constant  
 $\varepsilon$  – Emissivity (0-1)  
 $\alpha$  – Albedo  
 $L_f$  – Latent Heat of Fusion

$$Q_{\text{melt}} = Q_a - Q_{\text{bs}} + Q_e + Q_h + Q_{\text{precip}}$$

- $Q_{\text{melt}}$  total energy available to melt snow
- $Q_a$  longwave radiation  
 $f(\text{temperature})$
- $Q_{\text{bs}}$  longwave emission by soil  
considered constant ( $27 \text{ cal cm}^{-2} \text{ hr}^{-1}$ )
- $Q_e$  evaporation and sublimation  
 $f(\text{temperature, humidity, wind})$
- $Q_h$  sensible heat transfer due to turbulence  
 $f(\text{temperature, pressure, wind})$
- $Q_{\text{precip}}$  precipitation  
 $f(\text{precipitation, temperature})$

Assumes 1 cc of snow will melt for every 336 Joules  
(80 cal per gram of water)



Picture Adapted from: Tarboton 1996

HY Method accounts for cold content (heat deficit) within the snowpack.



- Based on SNOW-17 (Anderson 1968; 1973; and 2006)
- Melt occurs once heat deficit is overcome
- Melt rates ( $M$ ) based on Air Temperature and calibrated Melt Factors

- Melt under normal circumstances:

$$M = [M_f \cdot (T_a - MBASE) + 0.0125 \cdot P \cdot f_r \cdot T_r]$$

- Melt during rain events:

$$M = \sigma \cdot dt \cdot [(T_a + 273)^4 - 273^4] + 0.0125 \cdot P \cdot f_r \cdot T_r + 8.5 \cdot f_u \cdot (dt/6) \cdot [(rh \cdot e_{sat} - 6.11) + 0.00057 \cdot P_a \cdot T_a]$$

- where:

$M_f$  = melt factor, varies daily between a calibrated minimum and maximum value

$P$  = precipitation

$f_r$  = fraction of precipitation in form of rain

$f_u$  = wind function

$MBASE$  = temperature at which snow begins to melt



Temperature Index (TI)

$$Melt = M_f T_a dt$$

$$T_a \approx \left( \frac{LW_{\downarrow}}{\sigma \varepsilon_{air}} \right)^{1/4}$$

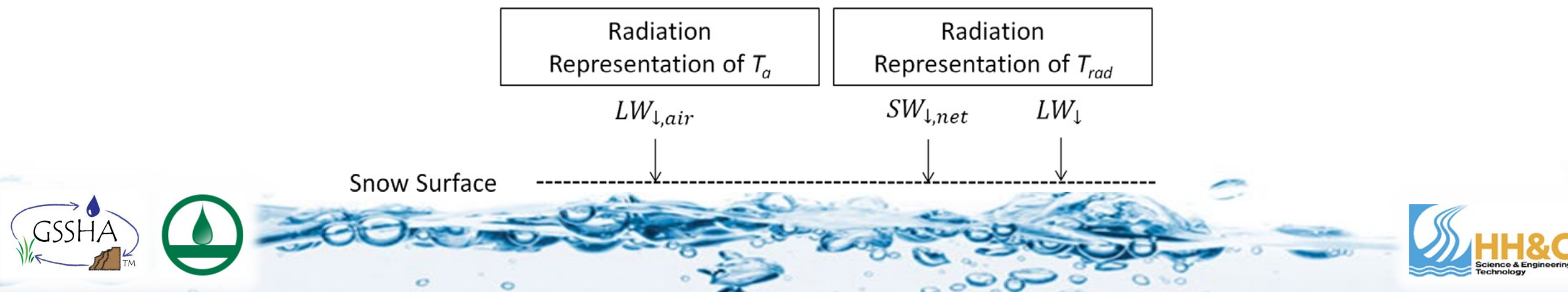
Requires:  
Temperature  
Precipitation

Radiation-Derived Temperature Index (RTI)

$$Melt = M_f T_{rad} dt$$

$$T_{rad} \approx \left( \frac{LW_{\downarrow} + SW_{\downarrow net}}{\sigma \varepsilon_{snow}} \right)^{1/4}$$

Requires:  
Temperature  
Precipitation  
Cloud Cover





## How to get $T_{rad}$

- Account for SW radiation and related reductions

$$SW_{\downarrow} = S_0 K_r K_v K_c K_{atm} K_s K_t$$

$S_0$ =Solar Constant

$K_r$ =ratio of actual earth-sun distance to mean earth-sun distance (fraction)

$K_v$ =vegetation

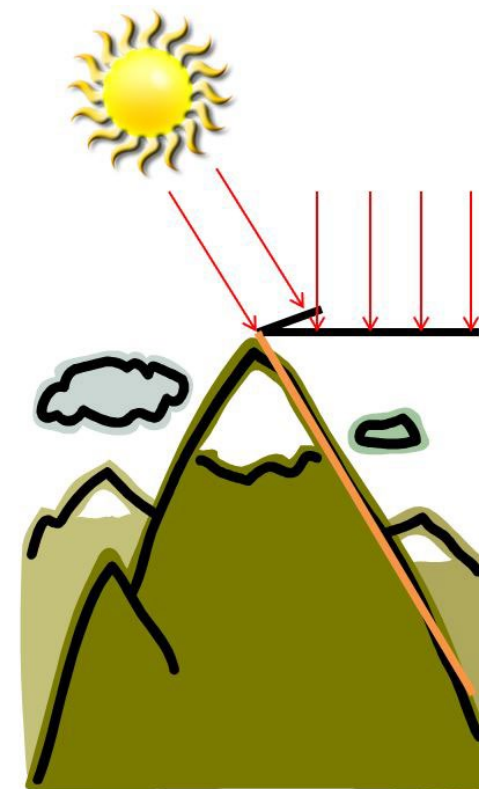
$K_c$ =clouds

$K_{atm}$ =atmospheric absorption and scattering

$K_t$ =topographic shading

$K_s$ =aspect angle

- Include snow albedo model (Henneman & Stefan, 1999)
- Account for LW radiation from clouds and canopy ( $LW_{\downarrow}$ )
  - LW clear sky, including emissivity of air (Bras, 1990)
  - Increase of LW due to clouds (TVA, 1972)
  - Adjustment of LW due to vegetation (Liston & Elder, 2006).



For more details see Follum et al. (2015)

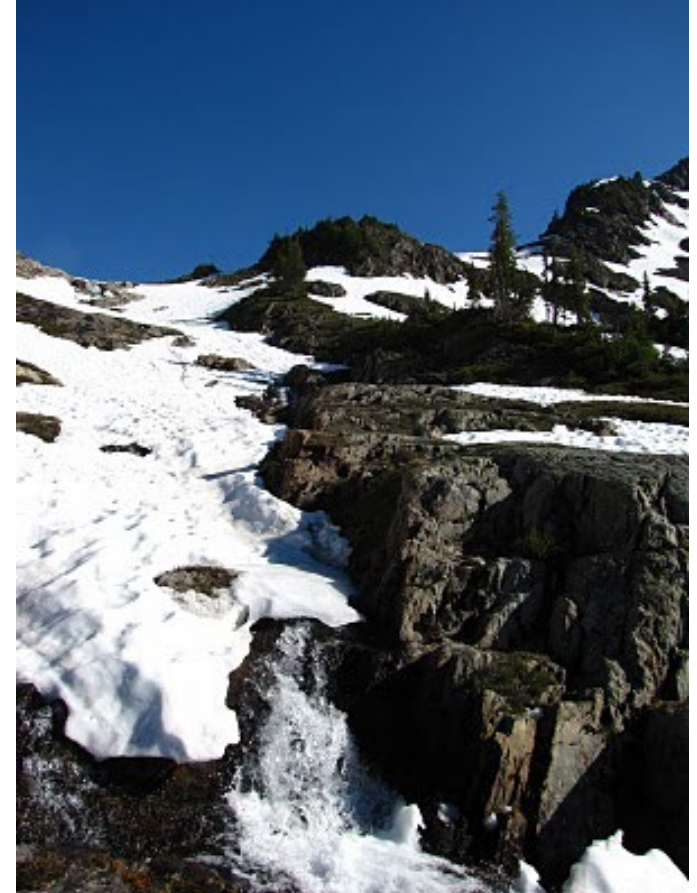
- Energy Balance
  - Uses energy balance algorithms to determine melt, but does not include Heat Deficit.
  - Typically underestimates SWE when topography not accounted for in the model.
- Temperature-Index
  - Uses temperature, precipitation, and calibrated parameters to simulate snow melt.
  - Incorporates the Heat Deficit / Snow-Pack Dynamics
  - Requires calibration (9 Parameters)
- Hybrid Energy Balance (**Default** in GSSHA)
  - Incorporates the Energy Balance melting algorithms
  - Incorporates the Heat Deficit / Snow-Pack Dynamics (4 Parameters)
- Radiation-Derived Temperature-Index Method
  - Same as TI method, but accounts for spatial heterogeneity in energy, and therefore produces a more accurate spatial representation of the snowpack.
  - Requires calibration (8+ Parameters)



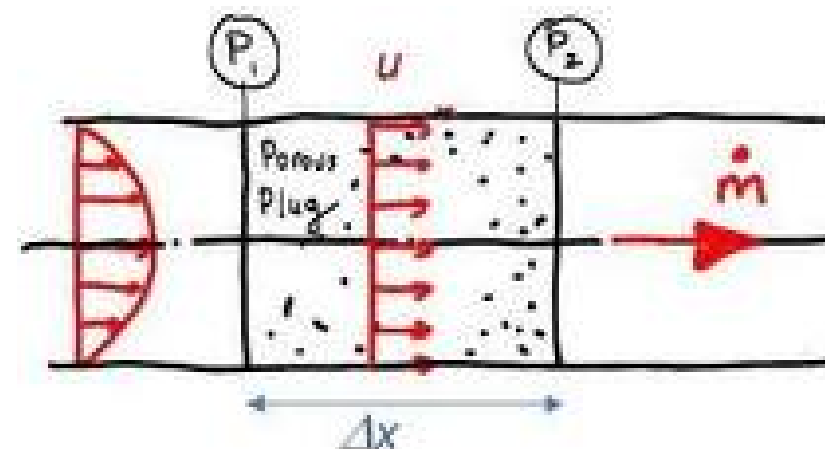
- Three Methods for Adjusting HMET with Elevation
  - SIMPLE: Define a constant temperature lapse rate, then GSSHA adjusts temperature. Relative humidity and pressure can also be adjusted. Typically used.
  - COMPLEX: Let GSSHA automatically adjust temperature, pressure, and relative humidity based on elevation using mean adiabatic lapse rate (MALR).
  - PUNT: Input raster-based forcing data from an atmospheric model, such as GFS (US) or ECMWF (European)



- Snow melt water is transported through the system in several ways:
  - Vertically through the snow-pack ❄️
  - Laterally through the snow-pack ❄️
  - Infiltration into soil (frozen/unfrozen) ❄️
  - Overland flow
  - Groundwater flow
  - Channel flow



- Flow through the Snow-pack is simulated Porous Media Flow.
  - A form of Darcy's Equation is typically used to determine flux through the snow-pack, both vertically and laterally.
  - Vertical flow is typically considered unsaturated flow.
  - Lateral flow through the the snow-pack is typically considered saturated Flow.
- GSSHA uses the SNAP Model (Albert 1998) to Determine Snow-pack Properties in each Computational Cell:
  - Saturation
  - Saturated / unsaturated hydraulic conductivity
  - Effective porosity

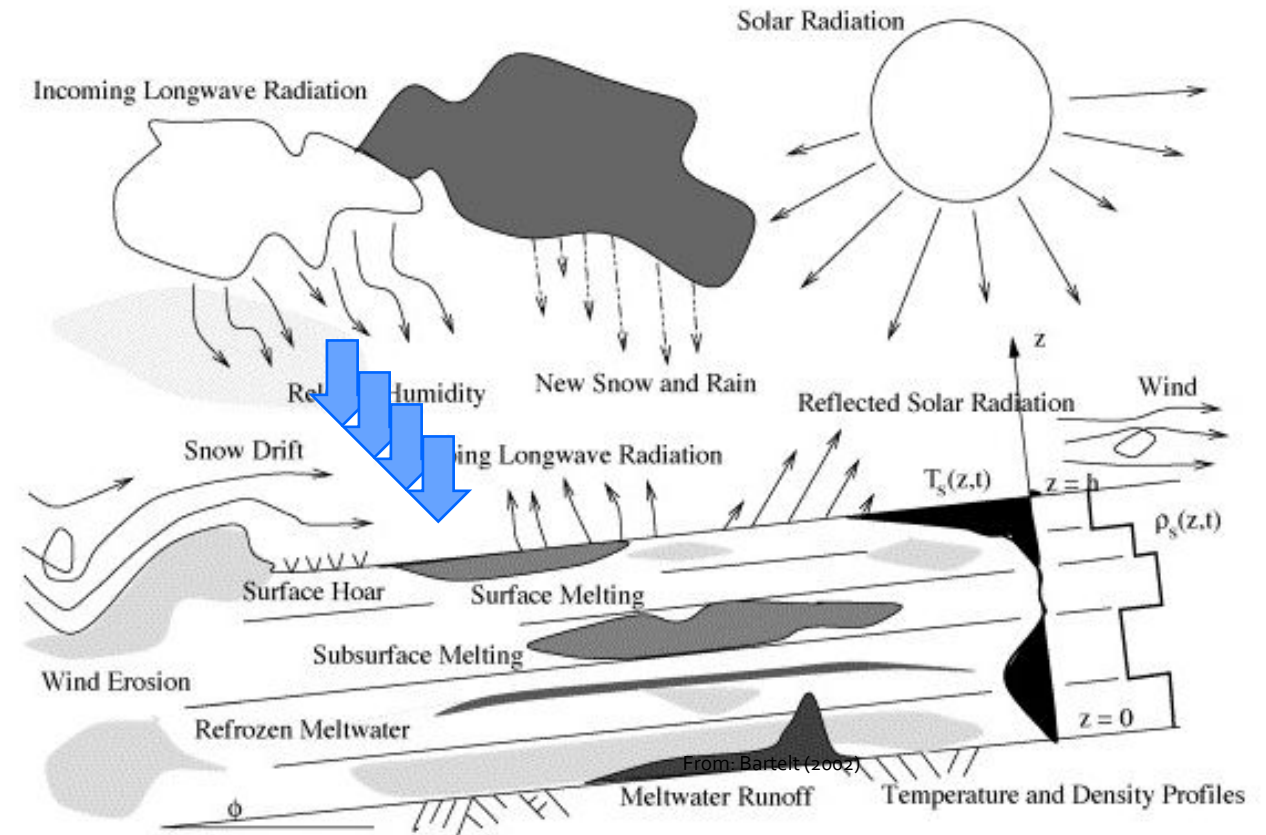




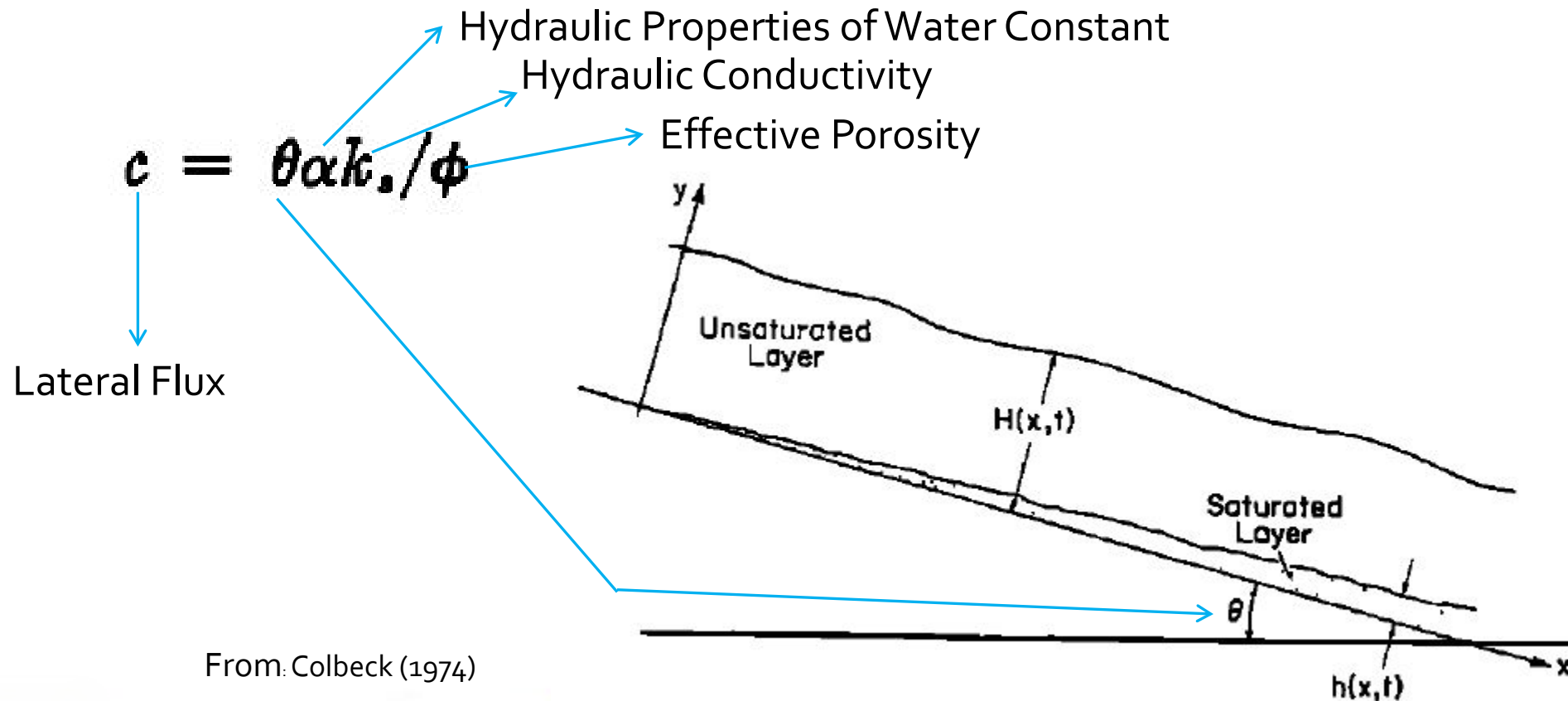
- Vertical Flow is considered unsaturated flow
  - Effective hydraulic conductivity ( $k_w$ ) changes with the degree of saturation ( $S$ ).

$$k_w = kS^n$$

- Effective porosity also changes with the degree of saturation.
- While flow is simulated through a single snow layer, multiple wetting fronts through the pack can occur – based on both Albert (1998) and Bengtsson (1981).

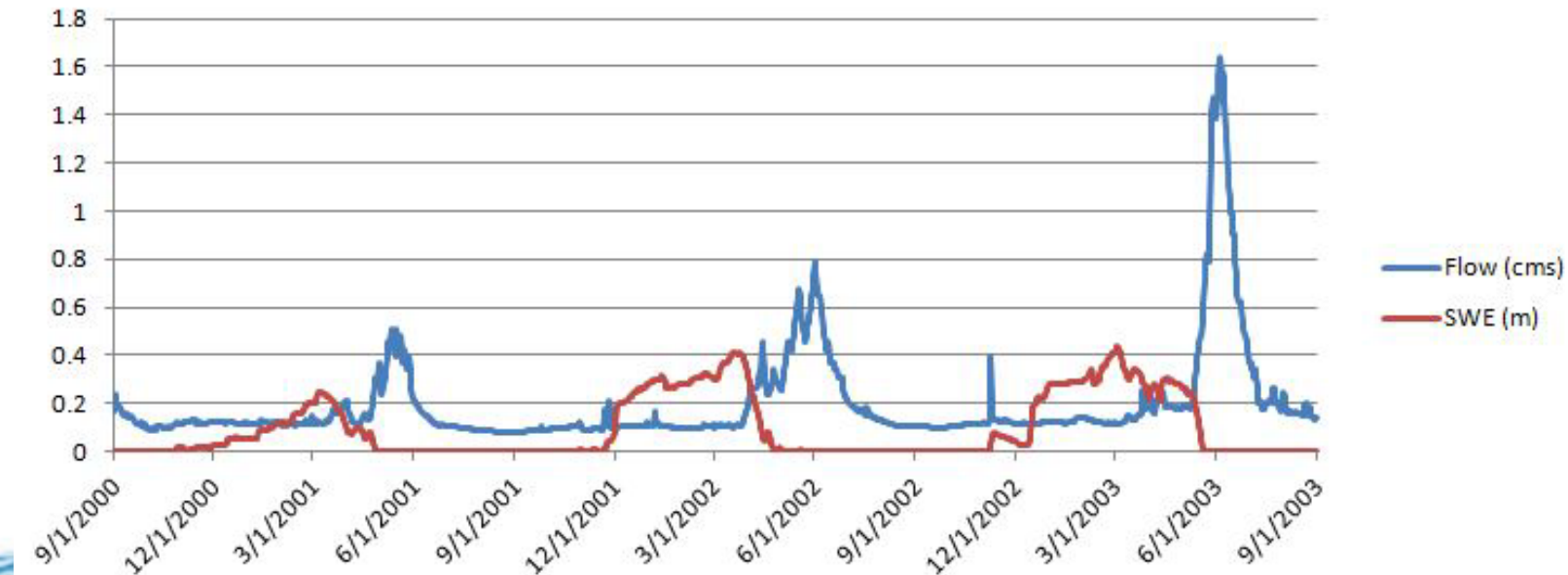


- Once the melt water reaches the ground it is transported as saturated Darcian flow according to methods developed by Colbeck (1974) to determine the flux between each cells.



- GSSHA uses a temperature-index method (CFGI model; Molnau & Bissel, 1983) to determine when the ground beneath a snow-pack is frozen, thus preventing infiltration.
  - See for more info: [http://www.gsshawiki.com/Frozen\\_Soil:Frozen\\_Soil](http://www.gsshawiki.com/Frozen_Soil:Frozen_Soil)
- The Handbook of Snow (Gray and Male, 1981) states that for long-term sustained water yields the groundwater flow component may be most important aspect considered.

Trout Creek Basin, CA

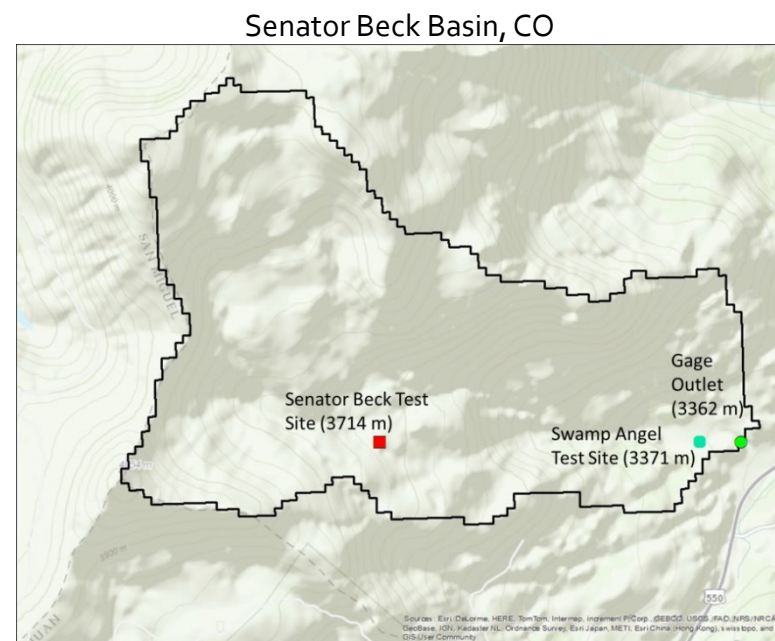




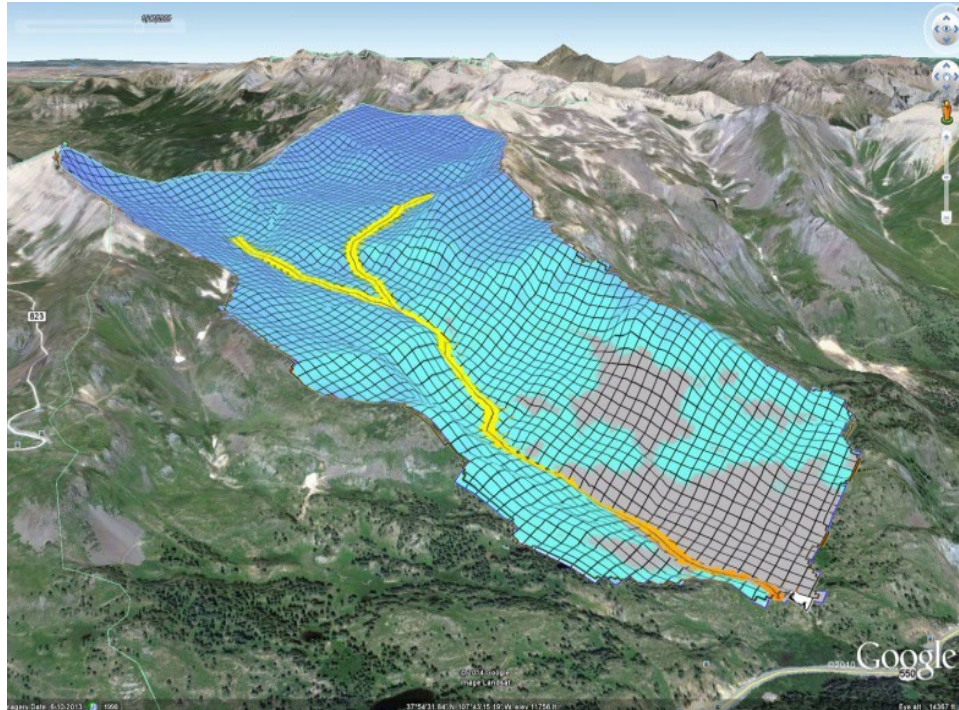
- Vertical Flow through Snow-Pack
- Lateral Flow through Snow-Pack
- Frozen Ground Simulation
- Existing routing mechanisms in GSSHA



- Test Basin: Senator Beck Basin, CO
  - Drainage Area: 2.91 km<sup>2</sup>, Elev: 3362 – 4118 m
  - Alpine terrain with primarily bare rock and tundra, with some forest below 3600-m
- Point Data Sources
  - Hydrometeorology at 3 sites from WY 2003 through current (Landry et al., 2014)
    - Temperature, precipitation, relative humidity, pressure, and wind speed
    - SWE, soil moisture, and shortwave (SW) radiation
  - Cloud cover data from Telluride Regional Airport (~16 km to northwest)
  - Streamflow data at outlet (Landry et al., 2014)
- Spatial Data Sources
  - SCA estimates from LandSat Imagery (31 images)
    - Spectral signatures processed using ERDAS Imagine
    - Assigned classifications: snow, no snow, and snow fringe
  - Elevation -> 1/3 Arc Second NED (Gesch et al., 2002)
    - projected to 30 m grid
  - Land Cover -> 2006 NLCD (Fry et al., 2011)
  - Soils Data -> SSURGO dataset (Soil Survey Staff, 2014)





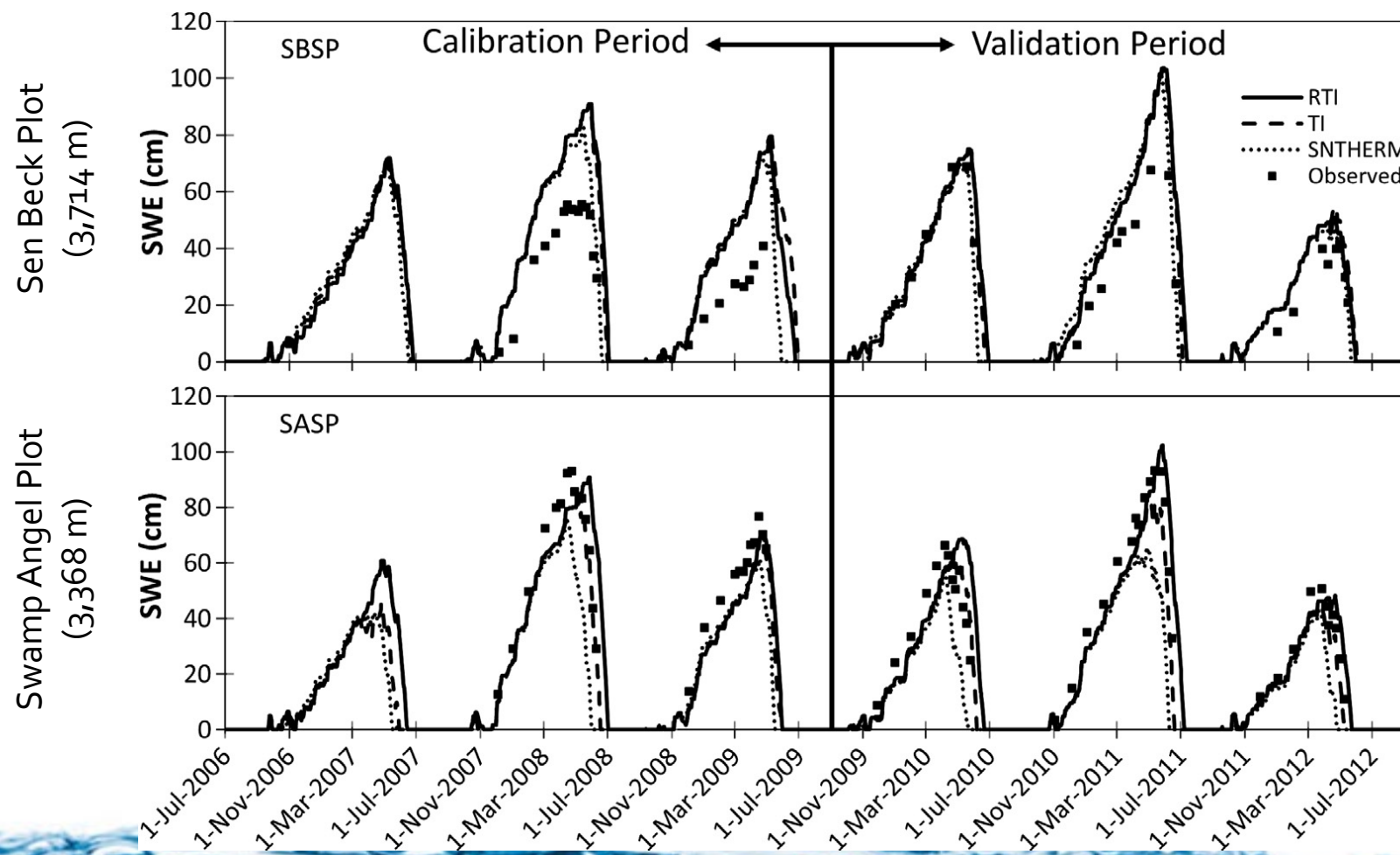


## Highlights:

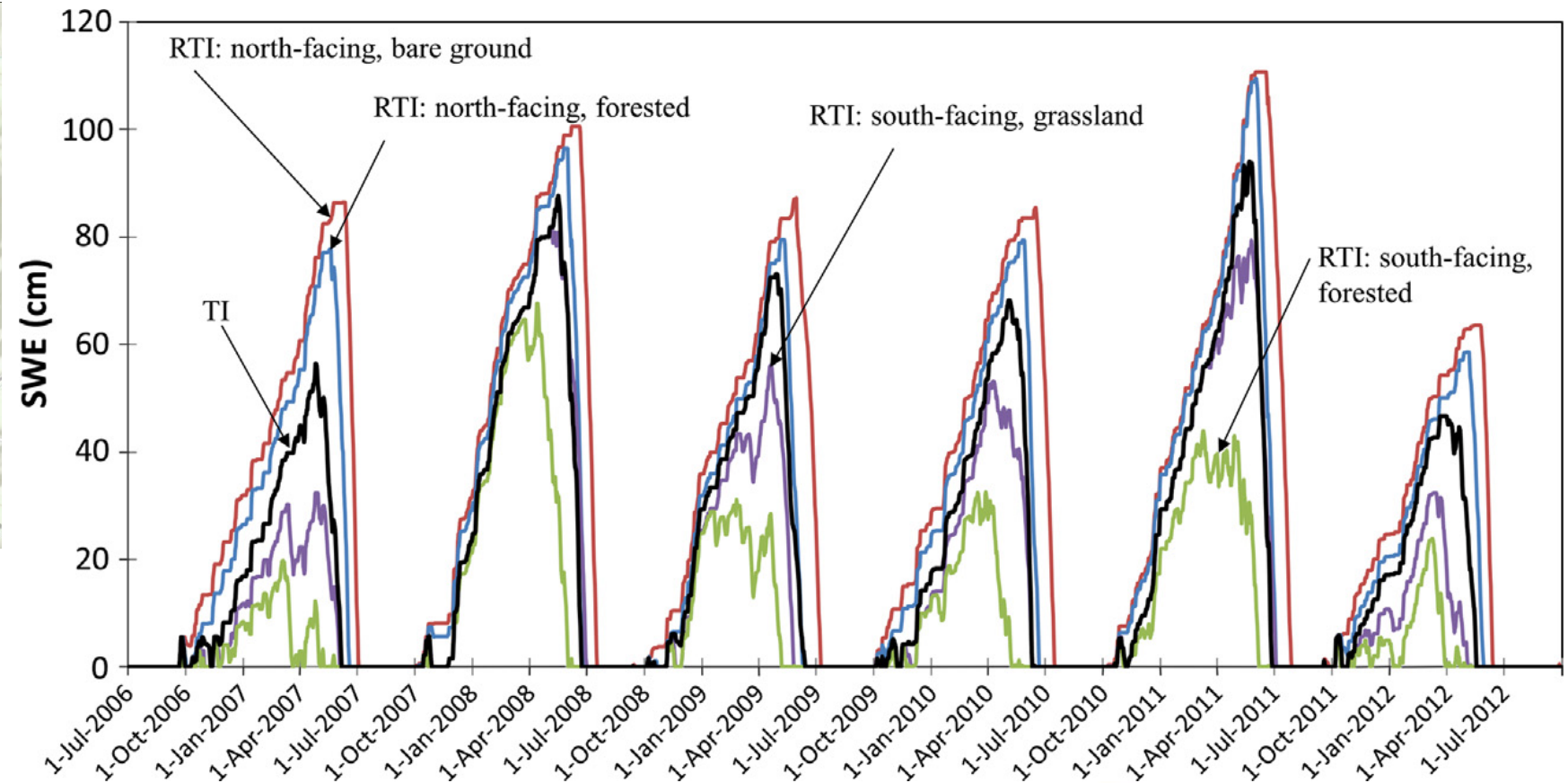
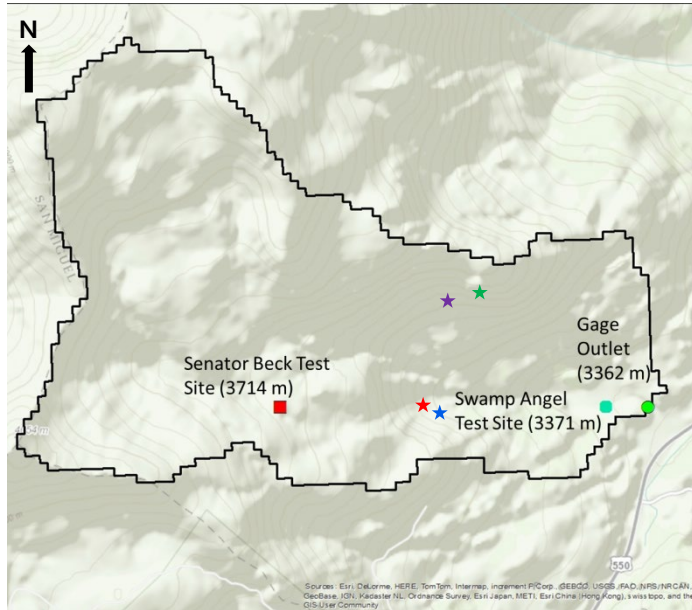
- Showed accurate snow simulation in an Alpine terrain (Follum et al., 2015)
- RTI model more accurate than TI and EB models



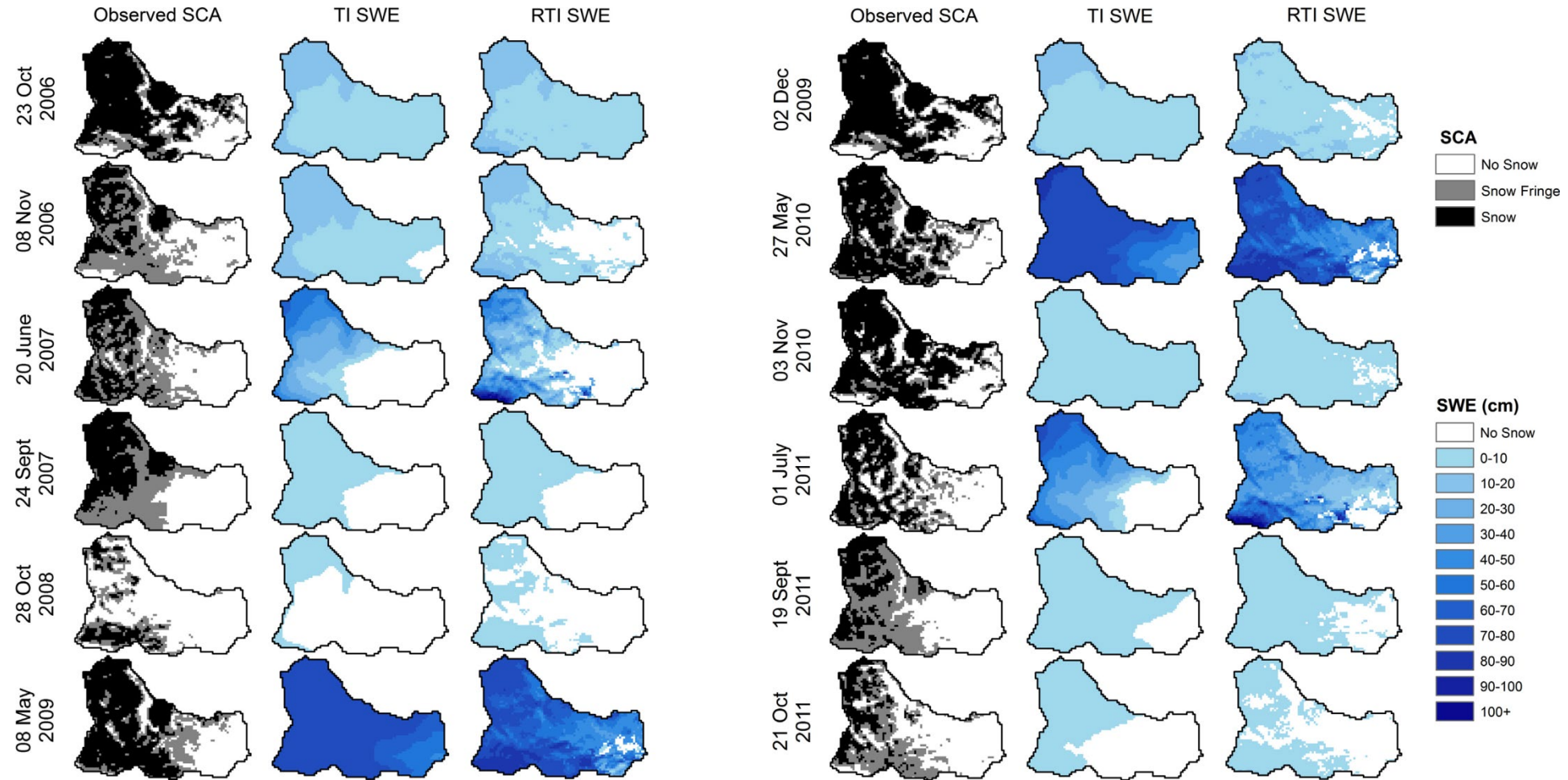
- Modest improvement in SWE at two gage sites



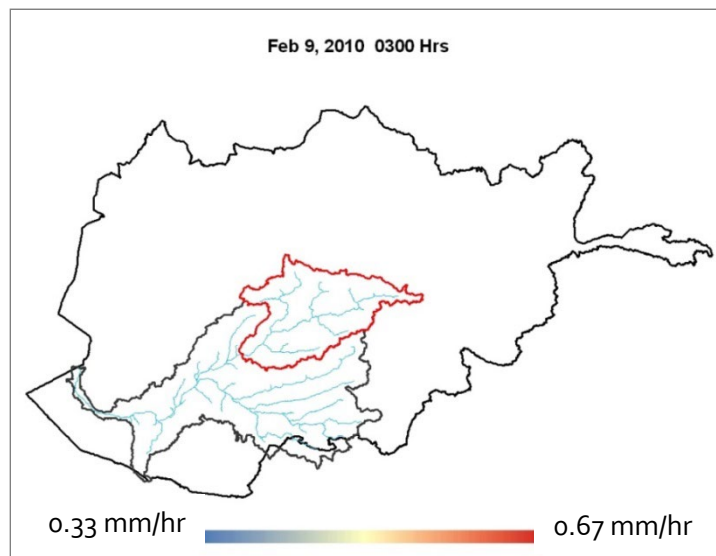
- Variability in SWE due to topography and vegetation









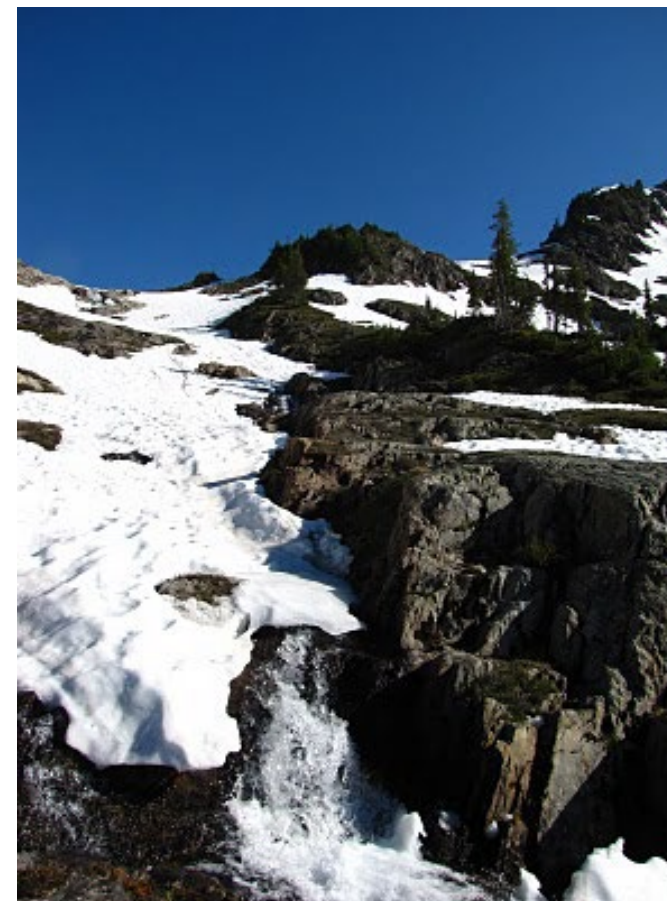


- Watershed-based
- Manual setup
- Limited forecasting window

Upper Helmand Basin Simulation: January  
– June 2010



- NRCS / USDA - <http://www.wcc.nrcs.usda.gov/>
  - SNOTEL, SCAN, Snowcoarses
- National Snow & Ice Data Center - <http://nsidc.org/>
- Remotely Sensed
  - Landsat, MODIS, AVHRR
- CZO's - <http://criticalzone.org/national/>
- Test Watersheds:
  - Senator Beck Basin, CO
  - Niwot Ridge, CO
  - Fraser Experimental Forest, CO
  - Loch-Vail, CO
  - Reynolds Experimental Watershed, ID
  - Sleepers River, VT
  - Hubbard Brook, NH
  - HJ Andrews, OR
  - Marmot Creek, Canada Rockies



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